

$$\text{Simplify: } \frac{2x}{x^2 - 7x + 12} \cdot \frac{x^2 - 9}{6x^2}.$$

Step 1: Factor each numerator and denominator completely

$$\frac{2 \cdot x}{(x-4)(x-3)} \cdot \frac{(x-3)(x+3)}{2 \cdot 3 \cdot x \cdot x}$$

Step 2: Multiply the numerators and denominators

$$\frac{\cancel{2} \cdot x \cdot \cancel{(x-3)}(x+3)}{\cancel{2} \cdot 3 \cdot x \cdot x \cdot \cancel{(x-3)}(x-4)}$$

Step 3 Simplify by dividing out common factors

$$\frac{x+3}{3x(x-4)}$$

Simplify:  $\frac{5x}{x^2+5x+6} \cdot \frac{x^2-4}{10x}$ .

$$\frac{5 \cdot x}{(x+3)(x+2)} \cdot \frac{(x-2)(x+2)}{2 \cdot 5 \cdot x}$$

$$\frac{\cancel{5} \cdot \cancel{x} \cdot (x-2)(\cancel{x+2})}{2 \cdot \cancel{5} \cdot \cancel{x} (x+3)(\cancel{x+2})}$$

$$\frac{x-2}{2(x+3)}$$

$$\text{Simplify: } \frac{9x^2}{x^2+11x+30} \cdot \frac{x^2-36}{3x^2}.$$

$$\begin{array}{r} \cancel{3 \cdot 3} \\ \cancel{3 \cdot x} \end{array} \quad \begin{array}{r} \cancel{(x-6)(x+6)} \\ \cancel{3 \cdot x \cdot x} \end{array}$$

$$\frac{\cancel{3 \cdot 3 \cdot x \cdot x} \cdot \cancel{(x-6)(x+6)}}{\cancel{3 \cdot x \cdot x} \cdot \cancel{(x+5)(x+6)}}$$

$$\frac{\cancel{3 \cdot 3 \cdot x \cdot x} \cdot \cancel{(x-6)(x+6)}}{\cancel{3 \cdot x \cdot x} \cdot \cancel{(x+5)(x+6)}}$$

$$\frac{3(x-6)}{x+5}$$

### **Divide rational expressions.**

- Step 1. Rewrite the division as the product of the first rational expression and the reciprocal of the second.
- Step 2. Factor the numerators and denominators completely.
- Step 3. Multiply the numerators and denominators together.
- Step 4. Simplify by dividing out common factors.

Divide

$$\frac{16a^7}{3b^5} \div \frac{8a^3}{6b}$$

$$\frac{16a^7}{3b^5} \cdot \frac{6b}{8a^3}$$

$$\frac{96a^7b}{24a^3b^5}$$

$$\frac{4a^4}{b^4}$$

$$\frac{3y+15}{y^7} \div \frac{y+5}{y^2}$$

$$\frac{3y+15}{y^7} \cdot \frac{y^2}{y+5}$$

$$\frac{3(y+5)}{y^7} \cdot \frac{y^2}{y+5}$$

$$\frac{3y^2(y+5)}{y^7(y+5)}$$
$$\frac{3}{y^5}$$

$$\frac{y^2-9}{y^2} \div \frac{y^5+3y^4}{y+2}$$

$$\frac{y^2-9}{y^2} \cdot \frac{y+2}{y^5+3y^4}$$

$$\frac{(y+3)(y-3)}{y^2} \cdot \frac{y+2}{y^4(y+3)}$$

$$\frac{(y+3)(y-3)(y+2)}{y^2 \cdot y^4(y+3)}$$

$$\frac{(y-3)(y+2)}{y^6}$$

$$\frac{y^3+3y}{y^2-9} \div \frac{y^2+5y-14}{y^2+4y-21}$$

$$\frac{y^3+3y}{y^2-9} \cdot \frac{y^2+4y-21}{y^2+5y-14}$$

$$\frac{y(y^2+3)}{(y+3)(y-3)} \cdot \frac{(y+7)(y-3)}{(y+7)(y-2)}$$

$$\frac{y(y^2+3)(y+7)(y-3)}{(y+3)(y-3)(y+7)(y-2)}$$

$$\frac{y(y^2+3)}{(y+3)(y-2)}$$

$$\frac{x^2-16}{x^2-10x+25} \div \frac{3x-12}{x^2-3x-10}$$

$$\frac{x^2-16}{x^2-10x+25} \cdot \frac{x^2-3x-10}{3x-12}$$

$$\frac{(x-4)(x+4)}{(x-5)(x-5)} \cdot \frac{(x-5)(x+2)}{3(x-4)}$$

$$\frac{(x-4)(x+4)(x-5)(x+2)}{3(x-5)(x-5)(x-4)}$$

$$\frac{(x+4)(x+2)}{3(x-5)}$$

$$\frac{x^2 - 7x - 8}{2x + 6} \div \frac{x^2 - 3x - 4}{4x + 12}$$

$$\frac{4y + 12}{2y - 10} \div \frac{y^2 - 9}{y^2 - y - 20}$$

$$\frac{2m^2 - 5m - 12}{m^2 - 10m + 24} \div \frac{4m^2 - 9}{m^2 - m + 18}$$

$$\frac{2m^2 - 5m - 12}{m^2 - 10m + 24} \cdot \frac{m^2 - m + 18}{4m^2 - 9}$$

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odd

$$\frac{(2m+3)(m-4)}{(m-6)(m-4)} \cdot \frac{m^2 - m + 18}{(2m-3)(2m+3)}$$

$$\frac{m^2 - m + 18}{(m-6)(2m-3)}$$

**Divide:** 
$$\frac{\frac{6x^2 - 7x + 2}{4x - 8}}{\frac{2x^2 - 7x + 3}{x^2 - 5x + 6}}$$

Simplify:  $\frac{\frac{y^2-36}{2y^2+11y-6}}{\frac{2y^2-2y-60}{8y-4}}$ .

Simplify: 
$$\frac{\frac{y^2-36}{2y^2+11y-6}}{\frac{2y^2-2y-60}{8y-4}}$$

Perform the indicated operations:  $\frac{3x-6}{4x-4} \cdot \frac{x^2+2x-3}{x^2-3x-10} \div \frac{2x+12}{8x+16}$ .

Perform the indicated operations:  $\frac{4m+4}{3m-15} \cdot \frac{m^2-3m-10}{m^2-4m-32} \div \frac{12m-36}{6m-48}$ .

Perform the indicated operations:  $\frac{2n^2+10n}{n-1} \div \frac{n^2+10n+24}{n^2+8n-9} \cdot \frac{n+4}{8n^2+12n}$ .